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Cascaded spintronic logic with low-dimensional carbon

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Remarkable breakthroughs have established the functionality of graphene and carbon nanotube transistors as replacements to silicon in conventional computing structures, and numerous spintronic logic gates have been presented. However, an efficient cascaded logic structure that exploits electron spin has not yet been demonstrated. In this work, we introduce and analyse a cascaded spintronic computing system composed solely of low-dimensional carbon materials. We propose a spintronic switch based on the recent discovery of negative magnetoresistance in graphene nanoribbons, and demonstrate its feasibility through tight-binding calculations of the band structure. Covalently connected carbon nanotubes create magnetic fields through graphene nanoribbons, cascading logic gates through incoherent spintronic switching. The exceptional material properties of carbon materials permit Terahertz operation and two orders of magnitude decrease in power-delay product compared to cutting-edge microprocessors. We hope to inspire the fabrication of these cascaded logic circuits to stimulate a transformative generation of energy-efficient computing.

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anipulation of the spin-degree of freedom for spintronic computing requires the invention of unconventional logic families to harness the unique mechanisms of spintronic switching devices¹⁻¹⁴. Cascading, one device directly driving another device, has been well known as a major challenge and fundamental requirement of a logic family since von Neumann's¹⁵ 1945 proposal for a stored-program electronic computer. If the input and output signals are not of the same type and magnitude, it is difficult to connect devices without an additional device for translation. This extra device consumes power, time and area, and severely degrades the utility of the logic family.

Here we present an alternative paradigm for computing: all-carbon spin logic. This cascaded logic family creatively applies recent nanotechnological advances to efficiently achieve high-performance computing using only low-dimensional carbon materials^{16–24}. A spintronic switching device is proposed utilizing the negative magnetoresistance of graphene nanoribbon (GNR) transistors^{25–29} and partially unzipped carbon nanotubes $(CNTs)^{30,31}$, unzipped^{30,32–35} from metallic CNT interconnect. These carbon gates can be cascaded directly; no additional intermediate devices are required between logic gates. The physical parameters necessary for proper switching operation are evaluated through mean-field tight-binding calculations of the band structure to enable an analysis of computational efficiency and to provide guidance for an experimental proof of concept. The results demonstrate the potential for compact all-carbon spin logic circuits with Terahertz operating speeds and two orders of magnitude improvement in power-delay product, thus motivating further investigation of the proposed device and computational structure.

Results

Device structure and physical operation. The active switching element is a zigzag GNR field-effect transistor with a constant gate voltage and two CNT control wires, as illustrated in Fig. 1. The gate voltage is held constant, and the GNR conductivity is therefore modulated solely by the magnetic fields generated by the CNTs. These magnetic fields can flip the orientation of the strong on-site magnetization at the GNR edges, which display local antiferromagnetic (AFM) ordering due to Hubbard interactions³⁶ (see Methods). As shown in Fig. 2, the magnetization at each edge is controlled by its neighbouring CNT, with magnetization decaying towards the centre of the GNR. In the absence of an external magnetic field or with edge magnetizations of opposite polarities, the GNR exhibits global AFM ordering in the ground state. Significantly, GNRs with edge magnetizations of

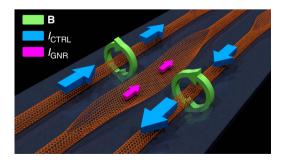


Figure 1 | **All-carbon spin logic gate.** Magnetoresistive GNR unzipped from carbon nanotube and controlled by two parallel CNTs on an insulating material above a metallic gate. As all voltages are held constant, all currents are unidirectional. The magnitudes and relative directions of the input CNT control currents I_{CTRL} determine the magnetic fields **B** and GNR edge magnetization, and thus the magnitude of the output current I_{GNR} .

the same polarity exhibit global ferromagnetic (FM) ordering in the ground state.

Mean-field tight-binding calculations show that the GNR global magnetic ordering determines the band structure, and therefore the conductivity. The Zeeman interaction can switch the magnetic ground state, causing spin-dependent band splitting. There are conduction modes in the FM state for all energies, but no conduction modes in the AFM state for Fermi energy $E_{\rm F}$ within the AFM state bandgap. By tuning $E_{\rm F}$ into the AFM bandgap through control of the gate voltage, the application of magnetic fields at the GNR edges causes a colossal change in conductivity, switching the GNR from the resistive AFM state to a conductive FM state. Importantly, if $E_{\rm F}$ is outside the AFM bandgap, conduction modes are always available, and switching of the magnetic ordering does not cause a change in conductivity. This is one possible explanation for the lack of magnetoresistance observed by Bai et al.²⁸ when applying an in-plane magnetic field to a GNR. It can be further noted that given the proximity between the CNTs and GNR, the attractive van der Waals and repulsive Casimir forces may alter the electronic wavefunctions and energy dispersion. However, these effects do not change the nature of the highly conductive CNT transport, nor the electron-electron repulsion among lattice sites. As a result, the spontaneous AFM ordering and edge magnetization are not sufficiently affected to alter the GNR magnetoresistance.

Edge effects and operation temperature. The spin-dependent band splitting is strongest with pristine zigzag edges³⁷ as achieved in ref. 35, enabling a spin-polarized current³⁸ and closing the energy gap for the GNR in the FM state as shown in Fig. 3. Local edge defects in quasi-pristine GNRs cause local perturbation in the magnetic ordering around these defects³⁷. However, the magnetic state is quickly regained within two unit cells (<1 nm) from the defect. As a result, the switching mechanism persists with defect spacing >3 nm, increasing the magnitude of the critical magnetic field for large defect density. As the magnetic

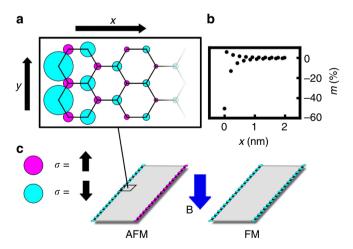


Figure 2 | Graphene nanoribbon edge magnetization. (a) On-site magnetization profile of a zigzag graphene edge. The magnetic field created by an adjacent CNT current causes strong on-site magnetization at the GNR edge. The colour of each circle represents the spin species, while the radius corresponds to the magnitude of the magnetization. (b) The on-site magnetization of each site in a unit cell as a function of distance from the edge. (c) Graphene nanoribbon edge magnetization in the absence and presence of an externally applied magnetic field. In the absence of a magnetic field, the GNR exhibits global AFM ordering with edges of opposite polarities. The application of a magnetic field aligns the edge polarities, achieving global FM ordering.

ordering originates from the GNR edges, it is not affected significantly by defects present away from the edges. In the case of very rough edges, a lack of sufficient contiguous zigzag portions to compensate for the presence of armchair edges may result in large switching fields.

Smooth GNRs with long contiguous stretches of pristine zigzag edges have been experimentally demonstrated³⁵. As defects affect the magnetization on the order of 1 nm around the defect location³⁷, this abundance of zigzag edges of 5 nm or larger elicits strong magnetic ordering. Sufficient contiguous zigzag edges between defects thus enable a persistence of the magnetic order.

Yazyev³⁹ indicated a GNR Curie temperature near 10 K, below which the spin correlation length grows exponentially. At temperatures around 70 K, correlation lengths are on the order of 10 nm, presenting a limitation for device operation. The correlation length approaches 1 nm at room temperature, making observation of the magnetization difficult in disordered systems. Therefore, low temperatures are desirable to minimize the required magnetic field and to ensure the manifestation of this effect in large samples. This concern may have been resolved, with magnetic order recently demonstrated in zigzag GNRs at room temperature⁴⁰.

Switching behaviour. We performed simulations of the proposed all-carbon spintronic switching device to determine the system and material parameters required to ensure feasibility. The magnetic instability energy is dependent on the GNR width (Supplementary Note 1), and determines the edge magnetic field required to switch the global ground state from AFM to FM ordering. As shown in Fig. 3c,d, the CNT current sufficient to overcome the magnetic instability energy is strongly affected by the proximity of the CNT control wires to the GNR edges. The current requirement can be tuned through control of the Hubbard U parameter. The required current ranges from exceptionally small magnitudes to significant fractions of an

Ampere, and can be minimized with a wide GNR positioned close to the CNT control wires. As the GNR width is increased, the magnetic instability energy decreases as nearly the inverse square of the width²⁵. For many *U* values and GNR/CNT geometries, the 20 μ A that can be passed through a single-walled CNT is sufficient to maintain the required switching current^{41–43}.

When the GNR switches from the AFM to the FM state, there is a massive change in conductance, as shown in Fig. 3f. The magnitude of the current through the GNR functions as the binary gate output, with binary 1 representing the large current of the conductive FM state and binary 0 representing the resistive AFM state. The GNR current flows through the CNT from which it was unzipped, and this binary CNT current is the input to cascaded GNR gates. It should be noted that unlike other spintronic logic proposals, logic gates can be cascaded directly through the carbon materials without requiring intermediate control or amplification circuitry.

Logic gates and system integration. The various combinations of input magnitudes and directions permit the computation of the logical OR and XOR operations. When there is no difference in magnetization between the edges of the GNR, the GNR is in the resistive AFM state and outputs a binary 0. Application of current through the CNTs can cause the GNR to switch into the FM state and output a binary 1. The OR logic function of Table 1 is computed by CNT currents oriented in opposite directions that create aligned on-site magnetization at the GNR edges. This OR gate thus enables a highly conductive FM state in the presence of current in at least one input CNT. In the XOR logic function of Table 2, the input currents are oriented in the same direction. Therefore, large currents flowing through both CNTs cause AFM ordering in the XOR gate, resulting in a small output current. This GNR switching device provides the functionality necessary for general-purpose computing, as the OR and XOR gates form a sufficient basis set to generate all binary functions.

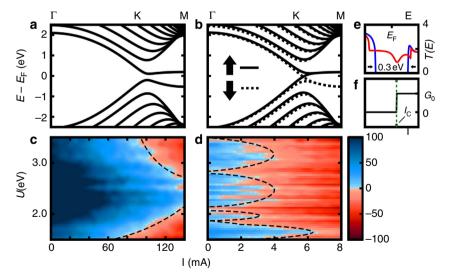


Figure 3 | **Magnetoresistive behaviour of GNR controlled by adjacent CNTs.** (**a**,**b**) Band diagrams for the AFM and FM global ordering of a 12-atom-wide zigzag GNR with zero current in the CNTs and Hubbard parameter U = 2.7 eV, as in equation (1) of Methods. In the global AFM state (**a**), there is a large gap between the valence and conduction bands, within which lies the Fermi energy, E_F . Therefore, there are no available conduction modes, and the conductance is zero. In the FM state (**b**), there is no bandgap and there is at least one conduction mode at all energies. (**c**,**d**) The magnetic instability energy in μ eV for zigzag GNRs with widths of (**c**) 20 nm and (**d**) 35 nm. The blue region designates a positive instability energy (the insulating AFM state), while the red region indicates negative instability energies (the conductive FM state). In the narrower GNR transistor, the axes of the CNTs are 10 nm from the GNR edge, while the wider GNR has CNTs placed 1nm away. The critical switching current, which depends on U, is denoted with a dashed line. (**e**) The transmission function $\overline{T}(E)$ of the AFM state defines the number of available conduction modes as well as the probability for an electron to travel across the device. Thus, for E_F values within the bandgap, the GNR conductance switches when the global ordering switches between the FM and AFM states. (**f**) A typical switching event, where the GNR conductance increases by G_0 when the CNT current overcomes the critical switching current I_C .

Nanofabrication trends suggest potential techniques for efficiently constructing cascaded all-carbon spin logic integrated circuits scaled up to perform complex computing tasks. Parallel and perpendicular CNTs can be laid out on an insulating surface⁴⁴ above a metallic material used as a constant universal gate voltage for the entire circuit. As shown in Fig. 4, a complex circuit composed of the logic gates of Fig. 1 can be created through selective CNT unzipping to form GNRs^{24,30,32-35}. Electrical connectivity between overlapping CNTs34,45,46 can be determined by the placement of an insulating material. The only external connections are to the supply voltage and user input/output ports (for example, keyboard, monitor and so on), possibly with vertical covalent contacts of the type described by Tour⁴⁷. All computing functionality is performed by the carbon materials alone, without the aid of external circuitry. As in other large-scale integrated circuits, fabrication imprecision (for example, misaligned CNTs, imperfect CNT junctions, edge defects and so on) can be tolerated provided that the GNR

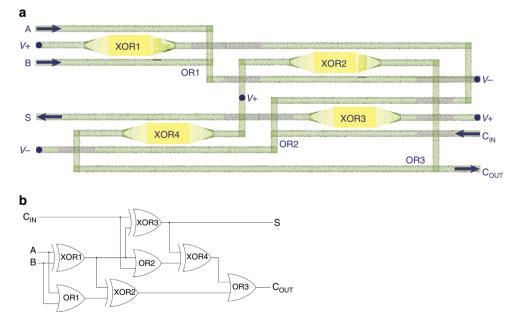
logic gates function properly and the electrical connectivity between CNTs is correct. Though the possibility of miniaturization is an important figure of merit for conventional computing structures, the atomic dimensions of CNTs and GNRs make the concept of down-scaling irrelevant for all-carbon spin logic.

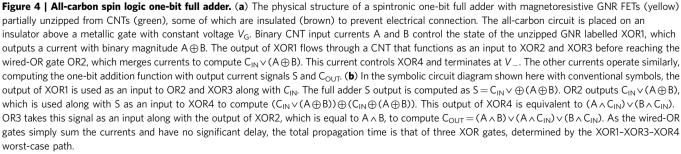
Cascaded all-carbon spin logic gates can be connected by routing the GNR output currents through the CNT control inputs of other GNR gates. Four XOR gates and three wired-OR gates are cascaded in Fig. 4 to realize a full adder, an essential computational function traditionally performed with 28 CMOS transistors (Supplementary Fig. 1 and Supplementary Table 1). The supply voltage nodes V_+ and V_- are held constant, thereby causing the polarities of all current paths to be constant. Binary switching results from changes in input current magnitudes due to changes in the output currents of other gates, without amplification, conversion or control circuitry. The output currents flow through the inputs of other logic and memory

Table 1 GNR OR gate truth table for input CNT control currents in opposite directions.				
I _A	I _B	State	Io	
0	0	AFM	0	
0	1	FM	1	
1	0	FM	1	
1	1	FM	1	

 Table 2 | GNR XOR gate truth table for input CNT control currents in the same direction.

IA	I _B	State	Io
0	0	AFM	0
0	1	FM	1
1	0	FM	1
1	1	AFM	0
1			





elements such as parity gates and toggle latches (Supplementary Figs 2 and 3, and Supplementary Table 2). These circuits provide traditional logic functionality with far fewer devices, enabling compact spintronic computing systems.

Discussion

While these circuits may be implemented with other materials exhibiting high conductivity and negative magnetoresistance, the exceptional properties of CNTs and GNRs make these structures ideal candidates for use in this logic family. Current is the state variable in all-carbon spin logic, enabling exceptionally fast computation with switching delay determined by electromagnetic wave propagation. This is in stark contrast to conventional computing systems in which voltage is the state variable, leading to CMOS switching and RLC interconnect delays limited by charge transfer and accumulation.

As described by Fig. 5, the GNR conductivity switches far faster than the signal can propagate through the CNTs⁴⁸. The all-carbon spin logic switching time $t_d = t_{mag} + t_{gnr} + t_{prop}$ is the summation of the times required for a CNT current to switch a magnetic field in a neighbouring GNR (t_{mag}), the GNR magnetoresistance to switch in response to a magnetic field (t_{enr}) and the electric field to propagate through the CNT to switch the current (t_{prop}) . The propagation time t_{prop} is significantly larger than t_{mag} and t_{gnr} , and therefore determines t_d . The electromagnetic wave propagation speed in a CNT is $v_{\rm f} = \frac{1}{\sqrt{L_{\rm K}C_{\rm Q}}} = 800 \,\rm km \, s^{-1}$, where $L_{\rm K} = 400 \,\rm pH \, nm^{-1}$ is the kinetic inductance and $C_Q = 0.4 \,\mathrm{aF}\,\mathrm{nm}^{-1}$ is the quantum capacitance⁴⁸. For 400 nm CNT interconnect length l_{cnv} the worst-case logic gate switching time is $t_d = t_{prop} = \frac{l_{ent}}{v_t} = 500$ fs. High-performance circuits operating with clock frequencies of 2 THz can therefore be realized. The average power dissipation per logic gate is $P = V_{supply}I_{average} = V_{supply}\frac{(l_{on} + l_{off})}{2} = 10 \,\mu\text{W}$, given a differential supply voltage $V_{supply} = V_+ - V_- = 1 \,\text{V}$ and an on-state current $L_{va} = L_0 \approx 20 \,\mu\text{A}$ sufficiently small to flow through a state current $I_{on} = I_C \approx 20 \,\mu\text{A}$ sufficiently small to flow through a single-walled CNT. The power-delay product for each gate, a metric of computing efficiency, can be determined for all-carbon spin logic as $PDP = Pt_d \approx 5 \times 10^{-18}$ J. This is approximately 100 times more energy-efficient than 22 nm CMOS.

Furthermore, the power dissipation of all-carbon spin logic is nearly independent of frequency, whereas conventional CMOS circuits dissipate increasing power as clock frequency is increased. This two orders of magnitude improvement outweighs the power costs of low-temperature operation and leaves significant room for second-order parasitic effects. This direct comparison can be made due to the absence of additional circuitry between logic gates, in contrast to other spintronic logic proposals. In addition, each GNR switching device in the all-carbon spin logic family performs the functionality of between four and twelve CMOS transistors. The one-bit full adder of Fig. 4, for example, has only

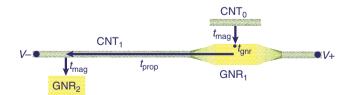


Figure 5 | Analysis of switching and propagation delay. Following a switch in the current through CNT_0 at a time t = 0, the magnetic field at the edge of GNR_1 switches at $t = t_{mag}$, the resistance of GNR_1 switches at $t = t_{mag} + t_{gnr}$ and the current through CNT_1 switches at $t = t_{mag} + t_{gnr} + t_{prop}$. This marks the end of one complete switching and propagation cycle, and is immediately followed by the switching of GNR_2 .

four active GNR gates and a propagation time of $3t_{\rm d}$, yielding a PDP of 6×10^{-17} J.

All-carbon spin logic permits the development of cascaded spintronic logic circuits composed solely of low-dimensional carbon materials without intermediate circuits between gates, resulting in compact circuits with reduced area that are far more efficient than CMOS. Though a complete all-carbon spin logic system is several years away from realization, currently available technology permits experimental proof of the concept as shown in Fig. 6. By exploiting the exotic behaviour of GNRs and CNTs, all-carbon spin logic enables a spintronic paradigm for the next generation of high-performance computing.

Methods

Hubbard tight-binding Hamiltonian. The tight-binding Hamiltonian for a zigzag-edged GNR is

$$\begin{split} \widehat{H} &= -\sum_{ij\sigma} \left(t_{ij} \widehat{c}_{i\sigma}^{\dagger} \widehat{c}_{j\sigma} + \text{h.c.} \right) + U \sum_{i} \left(\widehat{n}_{i\uparrow} \left\langle \widehat{n}_{i\downarrow} \right\rangle + \widehat{n}_{i\downarrow} \left\langle \widehat{n}_{i\uparrow} \right\rangle - \left\langle \widehat{n}_{i\uparrow} \right\rangle \left\langle \widehat{n}_{i\downarrow} \right\rangle \right) \\ &- g_{S} \mu_{\text{B}} m_{S} \sum_{i} B_{i}^{Z} \left(\widehat{n}_{i\uparrow} - \widehat{n}_{i\downarrow} \right), \end{split}$$
(1)

where t_{ij} is the transfer integral between orbitals localized at sites *i* and *j* of the GNR lattice, and $\hat{c}_{i\sigma}^{(i)}$ is the annihilation (creation) operator for an electron of spin σ at site *i*. Interactions up to the third nearest neighbour are considered, and the values for all transfer and overlap integrals are taken from set D of Hancock *et al.*³⁷. In the second term, which represents the Coulomb interaction between electrons, *U* is the repulsive Hubbard parameter and $\hat{n}_{i\sigma}$ is the on-site occupation of an electron with spin σ . In the mean-field approximation, the expectation of the on-site occupation is used to reduce the complexity of the Hamiltonian, which can be solved with iterative methods^{49,50}. Finally, the third term represents the Zeeman interaction, where g_S is the electron spin and B_i^Z is the *z*-component of the magnetic field at site *i*. The non-homogeneous magnetic field is generated by the Biot–Savart law and permeates everywhere in space, thereby affecting every atom in the GNR (not only the edges). The magnitudes of the transfer integrals due to the magnetic field.

Diagonalization and the secular equation. By taking advantage of the translational symmetry of a GNR, the \mathbf{k}^{th} component of the Hamiltonian for spin σ can be written as

$$\widehat{H}_{\sigma}(\mathbf{k}) = \widehat{H}_{0\sigma} + \widehat{V}_{\sigma} e^{i\mathbf{k}\cdot\mathbf{a}} + \widehat{V}_{\sigma}^{\dagger} e^{-i\mathbf{k}\cdot\mathbf{a}}$$
⁽²⁾

where $\hat{H}_{0\sigma}$ represents the interactions within one unit cell, and $\hat{V}_{\sigma}^{(\dagger)}$ is the interaction between one cell and the next (previous) unit cell at a displacement of **a** (-**a**). Each component of the single-particle states can be calculated by solving the secular equation

$$\hat{H}_{\sigma}\hat{c}^{\mu}_{\sigma} = \epsilon^{\mu}\hat{S}_{\sigma}\hat{c}^{\mu}_{\sigma}.$$
 (3)

Here \hat{c}^{μ}_{σ} is the eigenstate of spin σ corresponding to the energy ε^{μ} and \hat{S}_{σ} is the overlap matrix, which is the identity matrix in the investigated parameter set. The

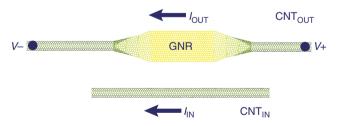


Figure 6 | Proposed proof-of-concept experiment. By measuring the change in I_{OUT} in response to a change in I_{IN} , the central component of all-carbon spin logic can be demonstrated. The carbon nanotube CNT_{OUT} can be partially unzipped such that a portion forms a GNR. A second CNT, CNT_{IN} , is then placed nearly parallel to CNT_{OUT} . A constant voltage should be applied across CNT_{OUT} . It is not necessary to achieve the dimensions described in this work; rather, to make the experiment more facile, CNT_{IN} must merely be close enough to the GNR to cause a measurable response in I_{OUT} when I_{IN} is varied. Furthermore, as shown in the figure, CNT_{IN} need not be as long as CNT_{OUT} , thereby preventing the CNTs from making contact even if the CNTs are not perfectly parallel.

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energies e_{x}^{k} corresponding to *N* states ζ_{x}^{k} where *N* is the number of sites in the unit cell, define the band structure of the GNR. At the GNR edges, we assume hydrogen passivation sp^{2} dangling bonds, which is the standard treatment of edges in simulations of transport through GNRs. As there is no dangling bond, there is no reconstruction other than a slight modification of the bond angle between H–C and C–C bonds. This has a negligible effect on the magnetization of the edges. In our calculations, we use 30,000 k points in the Brillouin zone.

Mean-field approximation. At zero temperature, the N lowest states are populated, and the occupation of the *i*th site in the unit cell is given by

$$\langle \hat{n}_{i\sigma} \rangle = \sum_{\mathbf{k}j}^{c_{\sigma}^{\mathbf{k}} < c_{F}} \widehat{\mathbf{S}}_{ij\sigma} \widehat{c}_{i\sigma}^{\mathbf{k}} \widehat{c}_{j\sigma}^{\mathbf{k}}$$
(4)

This value is used as an input to the Hamiltonian for the next iteration, and this process is repeated until the maximum change in occupation at any site is $<5 \times 10^{-7}$ per iteration.

Data availability. Data supporting the findings of this study are available from the authors on request.

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Author contributions

J.S.F. conceived of the switching device structure, designed the circuits and evaluated the logic family performance; A.G. characterized the magnetoresistance mechanism and evaluated the switching device behaviour; R.M.G. assisted in the materials selection and fabrication proposal; B.W.W. and J.-P.L. suggested the use of graphene for spintronic logic; J.-P.L. contributed to the device physics analysis; A.V.S., B.W.W., R.M.G., H.M. and G.M. contributed to the logic system analysis; A.T. contributed to the electromagnetic analysis; A.V.S. and J.-P.L. supervised the work; J.S.F., A.G. and R.M.G. prepared the manuscript, to which all authors contributed.

Additional information

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